

Page 154, equations (4.44) and (4.45)

Introducing (4.33) into l.h.s. of (4.43) and (4.40) into r.h.s. of (4.43) we obtain:

$$\sum_{\alpha=1}^n J^\alpha \vec{e}_\alpha = \sum_{p=1}^{n-h} J_p \sum_{\alpha=1}^n P^{p\alpha} \vec{e}_\alpha = \sum_{\alpha=1}^n \sum_{p=1}^{n-h} J_p P^{p\alpha} \vec{e}_\alpha.$$

Multiplying by \vec{e}_β ($\beta = 1, 2, \dots, n$) results in:

$$J^\beta = \sum_{p=1}^{n-h} J_p P^{p\beta}$$

which is (4.44).

Multiplying (4.43) by \vec{g}_r and referring to (A.85) we have:

$$\vec{J} \cdot \vec{g}_r = \sum_{p=1}^{n-h} J_p \vec{g}^p \cdot \vec{g}_r = J_1 \vec{g}^1 \cdot \vec{g}_r + \dots + J_r \vec{g}^r \cdot \vec{g}_r + \dots + J_{n-h} \vec{g}^{n-h} \cdot \vec{g}_r = J_r.$$

Then using (A.86) we obtain following expression:

$$J_r = \vec{J} \cdot \vec{g}_r = \vec{J} \cdot \sum_{p=1}^{n-h} g_{rp} \vec{g}^p = \sum_p g_{rp} \vec{J} \cdot \vec{g}^p$$

which can be further modified introducing (4.40):

$$= \sum_p g_{rp} \vec{J} \cdot \sum_{\alpha=1}^n P^{p\alpha} \vec{e}_\alpha = \sum_\alpha \sum_p g_{rp} P^{p\alpha} \vec{J} \cdot \vec{e}_\alpha.$$

Using (4.33) we finally arrive at:

$$J_r = \sum_\alpha \sum_p g_{rp} P^{p\alpha} J^\alpha$$

which is (4.45).