

Page 214, equation (4.333)

Writing (4.209) in space gradients gives:

$$\sum_{\beta=1}^{n-1} \sum_{\gamma=1}^n \omega_{\beta\gamma} \text{grad} \rho_{\gamma} = -\text{grad} P_n + \rho_n \text{grad} g_n - \rho_n \frac{\partial \hat{f}_n}{\partial T} \text{grad} T \quad (1)$$

and similarly for (4.208):

$$\sum_{\gamma=1}^n \omega_{\beta\gamma} \text{grad} \rho_{\gamma} = -\text{grad} P_{\beta} + \rho_{\beta} \text{grad} g_{\beta} - \rho_{\beta} \frac{\partial \hat{f}_{\beta}}{\partial T} \text{grad} T. \quad (2)$$

Henceforth, equilibrium is supposed and its symbol $^{\circ}$ omitted.

Insertion of (4.320), (4.327) and (4.317) into (1) gives (remember that $\text{grad} \rho \equiv \mathbf{h}$ and $\text{grad} T \equiv \mathbf{g}$):

$$\sum_{\beta=1}^{n-1} \mathbf{k}_{\beta} = -\rho_n (\mathbf{b}_n + \mathbf{i}_n) - \mathbf{k}_n + \rho_n \text{grad} g_n$$

and with respect to (4.328):

$$\rho_n (\mathbf{b}_n + \mathbf{i}_n) = \rho_n \text{grad} g_n. \quad (3)$$

Similar substitution into (2) results in

$$\mathbf{k}_{\beta} = \rho_{\beta} (\mathbf{b}_{\beta} + \mathbf{i}_{\beta}) + \mathbf{k}_{\beta} - \rho_{\beta} \text{grad} g_{\beta}, \quad \beta = 1, \dots, n-1$$

and

$$\text{grad} g_{\beta} = (\mathbf{b}_{\beta} + \mathbf{i}_{\beta}), \quad \beta = 1, \dots, n-1. \quad (4)$$

Equations (3) and (4) together (and not omitting the symbol $^{\circ}$) form (4.333).