

Page 148, equation (4.19)

Expression for $\partial\rho_\alpha\varphi/\partial t$ is modified substituting from (4.3) and (4.17); the summation convention is supposed:

$$\begin{aligned} \frac{\partial\rho_\alpha\varphi}{\partial t} &= \rho_\alpha \frac{\partial\varphi}{\partial t} + \varphi \frac{\partial\rho_\alpha}{\partial t} = \rho_\alpha \left(\overset{\alpha}{\varphi} - v_\alpha^i \frac{\partial\varphi}{\partial x^i} \right) + \varphi \left[r_\alpha - \frac{\partial}{\partial x^i} (\rho_\alpha v_\alpha^i) \right] \\ &= \rho_\alpha \overset{\alpha}{\varphi} - \rho_\alpha v_\alpha^i \frac{\partial\varphi}{\partial x^i} + \varphi r_\alpha - \varphi \frac{\partial}{\partial x^i} (\rho_\alpha v_\alpha^i) \\ &= \rho_\alpha \overset{\alpha}{\varphi} - \frac{\partial}{\partial x^i} (\varphi \rho_\alpha v_\alpha^i) + \varphi r_\alpha \equiv \rho_\alpha \overset{\alpha}{\varphi} - \operatorname{div} \rho_\alpha \varphi \mathbf{v}_\alpha + \varphi r_\alpha \end{aligned}$$

Eq. (4.19) follows immediately.